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# Characterization and physical properties of Li<sub>2</sub>O–CaF<sub>2</sub>–P<sub>2</sub>O<sub>5</sub> glass ceramics with Cr<sub>2</sub>O<sub>3</sub> as a nucleating agent—Physical properties

G. Murali Krishna, B. Anila Kumari, M. Srinivasa Reddy, N. Veeraiah\*

Department of Physics, Acharya Nagarjuna University - Nuzvid Campus, Nuzvid 521 201, India

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## Abstract

In this paper, studies on various physical properties, viz., dielectric properties (dielectric constant, loss tan  $\delta$ , a.c. conductivity  $\sigma$ ) over a wide range of frequency and temperature, optical absorption, ESR at liquid nitrogen temperature and magnetic susceptibility at room temperature of Li<sub>2</sub>O–CaF<sub>2</sub>–P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass ceramics, have been reported. The optical absorption, ESR and magnetic susceptibility studies indicate that the chromium ions exist in Cr<sup>5+</sup>, Cr<sup>4+</sup> and Cr<sup>6+</sup> states in addition to Cr<sup>3+</sup> state in these samples. The dielectric constant and loss variation with the concentration of Cr<sub>2</sub>O<sub>3</sub> have been explained on the basis of space charge polarization mechanism. The dielectric relaxation effects exhibited by these samples have been analysed by a graphical method and the spreading of dielectric relaxation has been established. The a.c. conductivity in the high-temperature region seems to be connected both with electronic and ionic movements.

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Keywords: Dielectric properties; Optical absorption; ESR spectra

# 1. Introduction

This paper is devoted to report the results of a systematic study on dielectric properties (viz., dielectric constant, loss and a.c. conductivity over a wide range of frequency and temperature), optical and magnetic properties of Li<sub>2</sub>O-CaF<sub>2</sub>-P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass ceramics. The studies on dielectric properties not only help in estimating the insulating strength but also give some additional information on structural aspects of the glass and glass-ceramic materials. Work along these lines has been carried out in recent years on a variety of inorganic glass systems vielding valuable information [1-5]. The objective of this study is to throw some light on the structural aspects of  $Li_2O-CaF_2-P_2O_5$ glass ceramics with Cr<sub>2</sub>O<sub>3</sub> as nucleating agent with the investigations on dielectric properties coupled with the data on ESR, optical absorption and magnetic susceptibilities studies.

\*Corresponding author. Fax: +918656235200.

E-mail address: nvr8@rediffmail.com (N. Veeraiah).

# 2. Experimental

For the present study, a particular composition (30-x)Li<sub>2</sub>O-10 CaF<sub>2</sub>-60 P<sub>2</sub>O<sub>5</sub>: x Cr<sub>2</sub>O<sub>3</sub> with five values of x ranging from 0 to 1.0 is chosen. The details of the compositions as reported in the Part I are:

- $C_0$ : 30 Li<sub>2</sub>O-10 CaF<sub>2</sub>-60 P<sub>2</sub>O<sub>5</sub>
- $C_2$ : 29.8 Li<sub>2</sub>O-10 CaF<sub>2</sub>-60 P<sub>2</sub>O<sub>5</sub>: 0.2 Cr<sub>2</sub>O<sub>3</sub>
- $C_4$ : 29.6 Li<sub>2</sub>O-10 CaF<sub>2</sub>-60 P<sub>2</sub>O<sub>5</sub>: 0.4 Cr<sub>2</sub>O<sub>3</sub>
- $C_6$ : 29.4 Li<sub>2</sub>O-10 CaF<sub>2</sub>-60 P<sub>2</sub>O<sub>5</sub>: 0.6 Cr<sub>2</sub>O<sub>3</sub>
- $C_8$ : 29.2 Li<sub>2</sub>O-10 CaF<sub>2</sub>-60 P<sub>2</sub>O<sub>5</sub>: 0.8 Cr<sub>2</sub>O<sub>3</sub>

 $C_{10}$ : 29.0  $Li_2O-10$   $CaF_2-60$   $P_2O_5$ : 1.0  $Cr_2O_3$ 

The techniques of the preparation and the characterization of the samples were reported earlier [5]. The optical absorption spectra of the glasses were recorded at room temperature in the wavelength range 300–800 nm up to a resolution of 0.1 nm using CARY 5E UV–VIS-NIR

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Spectrophotometer. The ESR spectra of the fine powders of the samples were recorded at liquid nitrogen temperature on JEOL JES-TES100 X-band EPR spectrometer. The samples used for optical and dielectric studies were prepared by suitable grinding and optical polishing to the dimensions of  $1 \text{ cm} \times 1 \text{ cm} \times 0.2 \text{ cm}$ . A thin layer of silver paint was applied on either side of the large-faces of the samples, in order to serve as electrodes for dielectric measurements. The dielectric measurements were made on LCR Meter (Hewlett-Packard Model-4263 B) in the temperature range 30–250 °C. The accuracy in the measurement of dielectric constant is ~0.001 and that of loss is ~10<sup>-4</sup>. The magnetic susceptibility measurements were made by Guoy's method using fine powders of the sample to an accuracy of  $10^{-6}$  emu.

## 3. Results and discussion

#### 3.1. Optical absorption

Fig. 1 shows the optical absorption spectra of Li<sub>2</sub>O– CaF<sub>2</sub>–P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass ceramics in the wavelength region 300–1500 nm; the absorption edge observed at 314 nm for the sample C<sub>0</sub> is observed to shift to 320 nm with the introduction of nucleating agent (0.2 mol%). When the content of Cr<sub>2</sub>O<sub>3</sub> is raised to 0.4 mol%, the edge is observed to shift towards further higher wavelength. When the concentration of the dopant is raised further (up to 0.8 mol%) the edge is gradually shifted towards lower wavelength. From the observed absorption edges, we have evaluated the optical band gaps ( $E_0$ ) of these samples by drawing Urbach plots (Fig. 1b) between  $(\alpha \hbar \omega)^{1/2}$  and  $\hbar \omega$  as per the equation,

$$\alpha(\omega)\hbar\omega = c(\hbar\omega - E_{\rm o})^2. \tag{1}$$

From the extrapolation of the linear portion of the curves of Fig. 1(b), the values of optical band gap ( $E_o$ ) are determined and presented in Table 1 along with the other pertinent data. The value of the optical band gap is observed to be the highest for the sample C<sub>8</sub>.

The spectrum of glass-ceramic sample C2 exhibited absorption bands at 452 and 655 nm identified due to the conventional transitions of  $Cr^{3+}$  ions. The intensity of these two bands is observed to increase when the concentration of crystallizing agent Cr<sub>2</sub>O<sub>3</sub> is raised to 0.4 mol%; additionally two feeble but clear kinks at about 680 and 717 nm have appeared on 650 nm band in the spectra of the samples C<sub>2</sub> and C<sub>4</sub>. For further increase in the content of Cr<sub>2</sub>O<sub>3</sub> a new band at about 355 nm, identified due to the excitation of  $CrO_4^{2-}$  (Cr (VI)) group is observed; a broad band with a meta-center at about 1020 nm could clearly be detected in the spectrum of the ceramic sample C<sub>8</sub>, this band is identified due to  ${}^{3}A_{2} \rightarrow {}^{3}T_{2}$  transition of Cr<sup>4+</sup> ions [6]. It may be worth mentioning here that we have recorded the optical absorption spectra of all the samples before crystallization; the spectra have exhibited only the conventional bands of  $Cr^{3+}$  ions.



Fig. 1. (a) Optical absorption spectra of  $Li_2O-CaF_2-P_2O_5$ :  $Cr_2O_3$  glass ceramics. (b) Urbech plot for evaluating optical band gap of  $Li_2O-CaF_2-P_2O_5$ :  $Cr_2O_3$  glass ceramics.

Using Tanabe–Sugano diagrams for  $d^3$  ion, the spectra have been analysed and the bands are assigned to  ${}^4A_2 \rightarrow {}^4T_1(F)$ ,  ${}^4A_2 \rightarrow {}^4T_2$  transitions, respectively. The corresponding LF parameters  $D_q$  (crystal field splitting energy) and *B* (Racah parameter, measure of the Coulomb repulsion among the 3*d* electrons of  $Cr^{3+}$  ion) have been evaluated and presented in Table 1. Using these values, the nephelauxetic ratio, i.e,  $\beta = B$  (complex)/*B* (free ion) is evaluated for all the glasses and also presented in Table 1; the value of  $\beta$  is observed to decrease with gradual increase in the concentration of chromium content in the ceramic sample from 0.4 to 0.8 mol%. These results point out that there is a gradual increase in the covalent environment for

Table 1
Summary of the data on optical absorption spectra of Li <sub>2</sub> O-CaF <sub>2</sub> -P <sub>2</sub> O <sub>5</sub> :Cr <sub>2</sub> O <sub>3</sub> glass ceramics

Glass	Cut-off wavelength (nm)	Optical band gap $E_0$ (eV)	Position of ${}^{4}A_{2} \rightarrow {}^{4}T_{1}(F)$ band (nm)	Position of ${}^{4}A_{2} \rightarrow {}^{4}T_{2}$ band (nm)	$D_q \ (\mathrm{cm}^{-1})$	$B (\mathrm{cm}^{-1})$	β
C <sub>0</sub>	314	3.55	_	_	_	_	_
$C_2$	319.4	3.5	452	655	1526	621	0.676
$\overline{C_4}$	324.3	3.4	456	664	1504	630	0.686
C <sub>6</sub>	308.4	3.575	451	643	1555	610	0.664
C <sub>8</sub>	298.7	3.675	449	637	1570	605	0.659
C <sub>10</sub>	304	3.625	453	648	1543	620	0.675

chromium ions in the glass-ceramic network. Additionally, a pair of weak narrow structures at 687 and 702 nm due to  ${}^{4}A_{2} \rightarrow {}^{2}T_{1}$  and  ${}^{4}A_{2} \rightarrow {}^{2}E$  (spin and parity forbidden) transitions, respectively, have also been located with a clear resolution on  ${}^{4}T_{2}$  band in the spectra of samples C<sub>2</sub> and C<sub>4</sub>. These bands appear due to the mixing of free ion wave functions with those of neighbour ions or the lattice vibrations. The essential condition for the mixing of free ion wave functions with those of neighbour ions or the lattice vibrations is that the symmetry associated with the centre of inversion is to be destroyed by the neighbours. Further, an increase in the widths of  ${}^{2}E$  and  ${}^{2}T_{1}$  bands could clearly be seen with a considerable shift towards higher wavelength with increase in the concentration of chromium ions from 0.2 to 0.4 mol%. Such an increase indicates an increase of disorder in the glass network, may be due to the increasing concentration of induced heterogeneous nucleation centres in the glass network that separate and reduce the long-range order of chromium and phosphate groups [7,8]. The optical absorption spectra of the ceramic samples exhibited an additional band at about 350 nm predicted due to the transition of  $Cr^{6+}$  ions at the expense of the bands due to  $Cr^{3+}$  ions when the concentration of the nucleating agent is increased beyond 0.4 mol%. These Cr (VI) ions exist in the form of  $Cr^{6^+}O^{2^-}$  centres in the frame of  $CrO_4^{2^-}$  groups [9].  $Cr^{6^+}$  ion belongs to  $d^0$  closed shell and does not have electrons in the *d* shell. Hence, this transition is due to charge transfer or the transformation of chromium ions from  $Cr^{6+}$  (3 $d^{0}2p^{6}$ ) state into  $\operatorname{Cr}^{5+}(3d^{1}2p^{5})$  state. In other words, the observed band is due to the excitation of p electron (involved in the ligand bonds of the  $t_1\pi$  symmetry) into the *d* shell. The energy level of  $\operatorname{Cr}^{5+}$  ion with  $3d^{1}2p^{5}$  electronic configuration splits into two states of symmetry, viz., 2e and  $4t_2$ . In view of this, we may expect two charge transfer bands corresponding to the following transitions from  $Cr^{6+}$  ions [10]:

$$\operatorname{CrO}_4^{2-}(3d^02p^6) \to \operatorname{CrO}_4^{3-}(3d^12p^5)(t_1^5, 2e)$$
  
and

$$\operatorname{CrO}_4^{2-}(3d^02p^6) \to \operatorname{CrO}_4^{3-}(3d^12p^5)(t_1^5, 4t_2)$$

Among these two, the band observed at about 350 nm can be ascribed to the first transition where as the band due to second transition (high-energy transition) band lies well below the cut-off wavelength [10]. Further, the spectrum of

the ceramic sample  $C_8$  exhibited a broad absorption hump in the region 900–1100 nm assigned to  ${}^{3}A_2 \rightarrow {}^{3}T_2$  transition of tetrahedrally coordinated  $Cr^{4+}$  ions [11]. Thus the analysis of the optical absorption spectra together with the XRD and EDS spectra (represented in Part I) point out that there is a possibility for the oxidation of  $Cr^{3+}$  ions into  $Cr^{6+}$  and  $Cr^{4+}$  ions during the crystallization despite the fact the original glass batch contains chromium ions in  $Cr^{3+}$  state. As mentioned before,  $Cr^{3+}$  ions occupy octahedral positions where as Cr (VI) ion may enter the glass network with  $CrO_4^{2-}$  structural units and alternate with  $PO_4$  units. A schematic illustration of phosphate network containing  $Cr^{3+}$  (in octahedral and tetrahedral) and  $Cr^{6+}$  ions tetrahedral positions is shown in Fig. 2.

The  $Cr^{3+}$  ions act as modifier similar to  $Li^+$  and  $Ca^{2+}$  ions in the glass-ceramic network. The lower the concentration of these modifier ions, the lower is the concentration of NBOs in the glass matrix. This leads to a decrease in the degree of localization of electrons there by decreasing the donor centres in the glass matrix. The presence of smaller concentration of these donor centres increases the optical band gap and shifts the absorption edge towards low wavelength side as observed (Fig. 1b).

## 3.2. Fluorescence studies

The fluorescence spectra (Fig. 3) of all the glass-ceramic samples is recorded at room temperature excited at 456 nm; the spectra exhibited a broad emission band in the spectral range of 750–800 nm. This band is identified due to  ${}^{4}T_{1} \rightarrow {}^{4}A_{2}$  transition of octahedral  $Cr^{3+}$  ions [12]. As the concentration of crystallizing agent is increased from 0.2 to 0.4 mol%, a considerable hike in the intensity of the peak with a shift in the meta-centre towards higher wavelength side could clearly be seen. For further increase in the concentration of  $Cr_{2}O_{3}$ , the emission band is faded away slowly. Thus the result of luminescence spectra point out that there is a decreasing concentration of  $Cr^{3+}$  ions (possibly due to conversion of these ions into  $Cr^{6+}$  state) from sample  $C_{4}$  to  $C_{8}$ .

## 3.3. ESR spectra

The ESR spectra of Li<sub>2</sub>O–CaF<sub>2</sub>–P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glassceramics samples recorded at liquid nitrogen temperature



Fig. 2. A schematic illustration of phosphate network containing  $Cr^{3+}$  (in octahedral) and  $Cr^{6+}$  ions tetrahedral positions in 3D.



Fig. 3. Luminescence spectra of  $Li_2O-CaF_2-P_2O_5$ :  $Cr_2O_3$  glass-ceramics recorded at room temperature with an excitation wavelength of 456 nm.

(Fig. 4) exhibit a remarkable dependence on the concentration of chromium ions. The spectra of the C<sub>2</sub> and C<sub>4</sub> ceramic samples showed a strong signal at g = 1.975 and a broad signal at about g = 4.73 due to Cr<sup>3+</sup> ions [13,14]. The separation between the two Kramers doublets, viz.,  $|\pm\frac{3}{2}\rangle$  and  $|\pm\frac{5}{2}\rangle$  leads to these two resonances. More precisely, as per the theory of Landry, the low field line at  $g\sim4.7$  is attributed to the isolated Cr<sup>3+</sup> ions that have local rhombic sites subjected to strong crystal field effects [15,16]. This signal arises mainly due to  $-3/2 \leftrightarrow +3/2$ , that are allowed due to low symmetry of Cr<sup>3+</sup> ions. Comparatively larger intensity of this low field peak exhibited by the spectrum of glass C<sub>4</sub> indicates higher concentrations of isolated Cr<sup>3+</sup> ions in this glass ceramic. The resonance



Fig. 4. ESR spectra of Li<sub>2</sub>O–CaF<sub>2</sub>–P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass-ceramics recorded at liquid nitrogen temperature.

signal at  $g \sim 1.975$ , arises due to the exchange coupling between  $Cr^{3+}-Cr^{3+}$  ion pairs. The intensity and the line width of this signal ( $g \sim 1.97$ ) are found to be the highest in the spectrum of the sample  $C_4$ ; such behaviour of this signal indicates the presence of larger concentration of  $Cr^{3+}$  ions in this sample. Absence of antiferromagnetic interactions between  $Cr^{3+}$  ions may also be responsible for the highest intensity of the signal to some extent in this sample [15].

As the concentration of the crystallizing agent  $Cr_2O_3$  is increased beyond 0.4 mol%, the  $Cr^{3+}$  signals are found to

Table 2 Data on magnetic susceptibility and other related parameters of Li<sub>2</sub>O–CaF<sub>2</sub>–P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass ceramics

Glass	$\chi (10^{-5}, emu)$	Total chromium ion concentration $N_i$ (10 <sup>21</sup> , ions/cm <sup>3</sup> )	$Cr^{3+}$ ion conc. evaluated from $\chi N'$ (10 <sup>21</sup> , ions/cm <sup>3</sup> )	$N'/N_{ m i}$
C <sub>2</sub>	5.178	2.823	2.540	0.896
$C_4$	10.272	5.307	5.041	0.949
C <sub>6</sub>	12.189	8.544	5.980	0.699
C <sub>8</sub>	12.397	11.698	6.082	0.520
C <sub>10</sub>	15.525	12.696	7.617	0.599

decay (obviously due to the oxidation of  $Cr^{3+}$  ions into higher valence states) and a new weak asymmetric signal at g = 1.983 appeared. This signal is identified due to  $Cr^{5+}$ ions [15,17]. Earlier it was identified that it is the J–T effect that gives raise this signal of  $Cr^{5+}$  ions [18]. Thus the analysis of the results of ESR spectra predicts a possible coexistence of chromium ions in  $Cr^{5+}$  state along with  $Cr^{3+}$ state in Li<sub>2</sub>O–CaF<sub>2</sub>–P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass ceramics especially when the concentration of the crystal stimulator is more than 0.4 mol%.

## 3.4. Magnetic susceptibility studies

Magnetic susceptibility of Li<sub>2</sub>O–CaF<sub>2</sub>–P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass-ceramics measured at room temperature is observed to increase gradually with increase in the content of Cr<sub>2</sub>O<sub>3</sub> (Table 2). From the values of magnetic susceptibilities, the concentration of Cr<sup>3+</sup> ion is evaluated (by taking magnetic moment of Cr<sup>3+</sup> ions as 3.8  $\mu_B$ ) and presented in Table 2. The magnetic properties of these glasses arise from the paramagnetic Cr<sup>3+</sup> (3d<sup>3</sup>) ions. The fraction (N'/N<sub>i</sub>), i.e., the ratio of Cr<sup>3+</sup> ions (N') to the total concentration of the chromium ions (N<sub>i</sub>), is found to be minimum for glassceramic sample C<sub>8</sub>; this result indicates the conversion of a high proportion of chromium ions from Cr<sup>3+</sup> state into Cr<sup>6+</sup> state in this sample.

## 3.5. Dielectric properties

The dielectric constant  $\varepsilon'$  and loss tan  $\delta$  at room temperature ( $\approx 30$  °C) of sample C<sub>0</sub> at 100 kHz are measured to be 8.07 and 0.0164, respectively; the values of  $\varepsilon'$  and tan  $\delta$  of all the glass-ceramic sample are found to increase slightly with decrease in frequency. Fig. 5 represents isotherms of dielectric constant  $(\varepsilon')$  with the concentration of Cr<sub>2</sub>O<sub>3</sub> of Li<sub>2</sub>O-CaF<sub>2</sub>-P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glassceramics measured at 10 kHz. The parameter,  $\varepsilon'$  is observed to increase with the increase in the concentration of  $Cr_2O_3$ from 0 to 0.4 mol% and for further increase (up to 0.8 mol%) the value of  $\varepsilon'$  is observed to decrease considerably at any temperature and frequency. The inset of Fig. 5 represents the variation of dielectric constant with temperature for the sample C<sub>4</sub> measured at different frequencies; the curves exhibit significant frequency dispersion.



Fig. 5. Isotherms of dielectric constant variation with the concentration of  $Cr_2O_3$  of  $Li_2O-CaF_2-P_2O_5$ :  $Cr_2O_3$  glass-ceramics measured at 10 kHz. Inset gives the variation of dielectric constant with temperature measured at different frequencies for the sample  $C_4$ .

The dielectric constant of a material is due to electronic, ionic, dipolar and space charge polarizations. Out of these, the space charge contribution depends on the purity and the perfection of the glasses. The considerable increase of  $\varepsilon'$ with temperature of the present glasses can only be attributed to space charge polarization due to the bonding defects produced by the modifiers [19]. With the successive increase of crystallizing agent Cr<sub>2</sub>O<sub>3</sub> from 0 to 0.4%, the values  $\varepsilon'$  are found to increase at any frequency and temperature indicating an increase in the space charge polarization. It is quite clear from optical absorption and ESR spectra, the chromium ions mostly exist in trivalent state in the ceramic samples, act as modifiers similar to Li<sup>+</sup> and Ca<sup>2+</sup> ions and generate bonding defects by breaking the P–O–P bonds. The defects thus produced create easy pathways for the migration of charges that would build up space charge polarization leading to an increase in the dielectric parameters as observed [20,21]. With the gradual increase of nucleating agent Cr<sub>2</sub>O<sub>3</sub> from 0.4 to 0.8 mol%, the values of  $\varepsilon'$  are found to decrease at any frequency indicating a decrease in the space charge polarization; such a decrease may be due to the presence of a part of chromium ions in Cr<sup>6+</sup> state which act as network former with CrO<sub>4</sub> structural units as evidenced from IR and Raman spectra. Further, there is a possibility for the cross linking of these CrO<sub>4</sub> units with PO<sub>4</sub> groups to form P-O-Cr bonds in the glass network as mentioned earlier. Such cross linkages obviously reduce the degree of disorder in the glass network and decreases the space charge polarization and leads to decrease in the values of dielectric constant of the glass ceramics.

A comparison plot of variation of dielectric loss  $\tan \delta$ with temperature, measured at a frequency of 1 kHz is presented in Fig. 6. The temperature dependence of  $\tan \delta$  of sample C<sub>2</sub> at different frequencies is shown as the inset of the same figure. The curves of all the glasses have exhibited distinct maxima; with increasing frequency the temperature



Fig. 6. A comparison plot of variation of dielectric loss with temperature for  $Li_2O-CaF_2-P_2O_5$ :  $Cr_2O_3$  glass ceramics at 1 kHz. Inset gives the variation of dielectric loss with temperature for glass-ceramic sample  $C_2$  at different frequencies.

maximum shifts towards higher temperature and with increasing temperature the frequency maximum shifts towards higher frequency, indicating the dielectric relaxation character of dielectric losses of these glasses. Further, the observations on dielectric loss variation with temperature for different concentrations of  $Cr_2O_3$  clearly show a decrease in the broadness and  $(\tan \delta)_{max}$  of relaxation curves with increase in the concentration of  $Cr_2O_3$  from 0.4 to 0.8 mol%.

Using the relation

$$f = f_0 \exp(-W_d/KT), \tag{1'}$$

the effective activation energy,  $W_d$ , for the dipoles is calculated for all the glass-ceramic samples and presented in Table 3 along with the other relevant data on dielectric loss; the activation energy is found to be the highest for the sample C<sub>8</sub>.

The observed dielectric relaxation effects in these ceramic samples may be attributed to association of divalent  $Ca^{2+}$  ions with a pair of  $PO_2^-$  in analogy with the mechanism—association of divalent positive ion with a pair of cationic vacancies—as was reported for a number of conventional glasses, glass ceramics and crystals containing divalent positive ions [22]. Although the Cole–Cole plot is very useful tool for describing relaxation effects, it is more convenient to determine the relaxation parameters by a graphical method suggested by Cole [23]. Combination of the conventional Debye's relations,

$$\varepsilon'(\omega) = \varepsilon_{\infty} + \frac{\varepsilon_{\rm s} - \varepsilon_{\infty}}{1 + \omega^2 \tau^2},\tag{2}$$

$$\varepsilon''(\omega) = \frac{(\varepsilon_{\rm s} - \varepsilon_{\infty})\omega\tau}{1 + \omega^2\tau^2},\tag{3}$$

gives rise to

$$\varepsilon''(\omega)\omega = \frac{(\varepsilon_{\rm s} - \varepsilon_{\infty})\omega\tau}{1 + \omega^2\tau^2} = \frac{1}{\tau}(\varepsilon_{\rm s} - \varepsilon'(\omega)),\tag{4}$$

$$\varepsilon''(\omega)/\omega = \frac{(\varepsilon_{\rm s} - \varepsilon_{\infty})\tau}{1 + \omega^2 \tau^2} = \tau(\varepsilon'(\omega) - \varepsilon_{\infty})).$$
(5)

Eqs. (4) and (5) yield straight lines with slope  $1/\tau$  and  $\tau$ , respectively. In the present measurements for one of the ceramic samples, viz., C<sub>4</sub>, the plots between  $\varepsilon''(\omega)\omega$  vs.  $\varepsilon'(\omega)$  and  $\varepsilon''(\omega)\omega$  vs.  $\varepsilon'(\omega)$  are shown in Fig. 7. The plots observed to be straight lines, however slight deviation from the straight line is observed in the low-frequency region.

Table 3			
Data on dielectric loss	of Li <sub>2</sub> O-CaF <sub>2</sub> -P <sub>2</sub> O <sub>5</sub> :	Cr <sub>2</sub> O <sub>3</sub> glass	ceramics

Sample	$(\tan \delta)_{\max avg}$	Temp. region of relaxation (°C)	Activation energy for dipoles (eV)
C <sub>0</sub>	0.032	70–128	2.92
$C_2$	0.035	60-119	2.65
$C_4$	0.038	50-110	2.57
C <sub>6</sub>	0.029	80-134	2.95
C <sub>8</sub>	0.022	102-150	3.10
C <sub>10</sub>	0.026	90-142	2.96

Such deviation suggests spreading of relaxation times. Graphs drawn for other glasses have also exhibited nearly the same behaviour. Thus the graphical analysis also indicates that in addition to the  $Ca^{2+1}$  ions, there are other types of ions that are contributing to the relaxation effects. The  $Cr^{5+}$  ( $d^1$ ) (probably other than those positioned in tetrahedral sites) ions also participate in dielectric relaxation effects. Earlier studies on the glasses containing  $d^1$  ions like  $W^{5+}$ ,  $V^{4+}$ ,  $Ti^{3+}$ ,  $Mo^{5+}$ , etc., showed that these ions act as electric dipoles and contribute to the dielectric relaxation effects [24-26]. If a part of chromium ions exists in  $\operatorname{Cr}^{5+}(d^1)$  state (even in small concentration), they may also contribute to the relaxation effects in addition to the  $Ca^{2+}$  ions and lead to the spreading of relaxation effects. In other words, the analysis further hints out that there is a possible presence of chromium ions in Cr<sup>5+</sup> state also in these samples as was indicated by the ESR spectra. The value of the effective activation energy associated with the dipoles is observed to increase with increase in the content of crystal stimulator from 0.4 to 0.8 mol% in the ceramic samples (Table 3); this observation points out a decreasing freedom for dipoles to orient in the field direction, obviously due to decreasing degree of disorder in the glass network.

The a.c. conductivity  $\sigma_{ac}$  is calculated at different temperatures using the equation:

$$\sigma_{\rm ac} = \omega \varepsilon' \varepsilon_{\rm o} \, \tan \, \delta, \tag{6}$$

where  $\varepsilon_{o}$  is the vacuum dielectric constant for different frequencies for all the glass ceramics and its variation at 10 kHz with 1/T is shown in Fig. 6. From these plots, the



Fig. 7. Variation of the quantities  $\epsilon''\omega$  and  $\epsilon''/\omega$  with  $\epsilon'$  of the sample C4 at 80 °C.

activation energy for the conduction in the high-temperature region over which a near linear dependence of  $\log \sigma_{ac}$ with 1/T could be observed is evaluated and presented in Table 4; the activation energy is found to be the lowest for sample  $C_4$  and highest for sample  $C_8$ . When a plot is made between  $\log \sigma(\omega)$  vs. activation energy for conduction (in the high-temperature region) a near linear relationship is observed (inset (a) of Fig. 8); this observation suggests that the conductivity enhancement is directly related to the increasing mobility of the charge carriers in the hightemperature region [27]. Since the alkali earth ions, viz.,  $Ca^{2+}$  ions are much less mobile than the lithium ions, the Ca<sup>2+</sup> ions may therefore be regarded as virtually immobile within the time window of hopping processes of Li<sup>+</sup> ions [28]. Hence, the contribution to the conductivity in the present glass-ceramic samples in the high-temperature region is mainly due to the mobility of monovalent lighter lithium ions. The conductivity isotherms as a function of the concentration of nucleating agent passes through a maximum at x = 0.4 mol% (inset (b) of Fig. 8). The mobile electrons, or polarons, involved in the process of transfer from  $Cr^{3+}$  to  $Cr^{6+}$ , are attracted by the oppositely charged Li<sup>+</sup> ions. This cation-polaron pair moves together as a neutral entity. As expected, the migration of this pair is not associated with any net displacement of the charge and thus does not contribute to electrical conductivity. As a result, we expect a decrease in the conductivity, as observed in the zone II of the plots [29].

The low-temperature part of the conductivity (a near temperature independent part, as in the case of present glasses) can be explained on the basis of quantum mechanical tunneling model [30] similar to many other glass systems reported recently from our laboratory [31–33]. The value of  $N(E_{\rm F})$ , i.e., the density of the defect energy states near the Fermi level, is evaluated using the equation [30]

$$\sigma(\omega) = \eta e^2 KT [NE_F]^2 \alpha^{-5} \omega \left[ \ln \frac{v_{\rm ph}}{\omega} \right]^4, \tag{7}$$

where  $\alpha$  is the electronic wave function decay constant and its average value is determined from  $\sigma_{ac} = e^{-2\alpha Ri}$ ,  $v_{ph}$  is phonon frequency (~5 × 1012 Hz), and  $\eta = \pi/3$  (Austin and Mott),  $\eta = 3.66\pi 2/6$  (Butcher and Hyden),  $\eta = \pi 4/96$ (Pollak) and presented in Table 4.

Table 4
Summary of results on ac conductivity of Li <sub>2</sub> O-CaF <sub>2</sub> -P <sub>2</sub> O <sub>5</sub> : Cr <sub>2</sub> O <sub>3</sub> glass
ceramics

Sample	$N(E_{\rm F})$ in (10 <sup>2</sup>	AE for			
	Austin-Mott	Butcher-Hyden	Pollak	conduction (eV)	
$\overline{C_0}$	6.89	3.65	6.99	0.215	
$\tilde{C_2}$	7.45	3.11	7.57	0.194	
$\overline{C_4}$	8.64	2.81	8.77	0.185	
C <sub>6</sub>	6.25	2.32	6.35	0.228	
C <sub>8</sub>	5.12	1.89	5.21	0.276	
C <sub>10</sub>	5.27	2.31	5.35	0.258	



Fig. 8. A comparison plot of variation of a.c. conductivity with 1/T at 10 kHz for CaF<sub>2</sub>-Li<sub>2</sub>O-P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass ceramics. Inset (a) represents the variation of conductivity with the activation energy and (b) shows the variation of conductivity isotherms with the concentration of Cr<sub>2</sub>O<sub>3</sub> measured at 10 kHz.

The value of  $N(E_F)$  is found to decrease with increase in the concentration of  $Cr_2O_3$  from 0.4 to 0.8 mol% indicating a gradual increase in the rigidity of the ceramic sample.

If the applied field is an alternating field, the specific dielectric loss, i.e., the loss per unit volume of the dielectric is given by

$$\rho_1 = E^2 \omega \varepsilon' \varepsilon_0 \, \tan \delta \, W/m^3. \tag{8}$$

This equation indicates that the higher the values of  $\varepsilon' \tan \delta$  of the glass at a given frequency, higher are the values of  $\rho_1$ . The dielectric breakdown strength is in fact inversely proportional to the specific dielectric loss represented by Eq. (8). Our observations on dielectric parameters of Li<sub>2</sub>O-CaF<sub>2</sub>-P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass ceramics, as mentioned earlier, indicate, the rate of increase of  $\varepsilon' \tan \delta$  with temperature is the lowest for the sample C<sub>8</sub>; the breakdown strength, which is inversely proportional to  $\varepsilon' \tan \delta$  is therefore expected to be the highest when compared with the other glass ceramics. Thus the experiments on the dielectric breakdown strength of Li<sub>2</sub>O-CaF<sub>2</sub>-P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass ceramics reveal that the sample C<sub>8</sub> possesses high electrical insulating strength among all other samples studied.

# 4. Conclusions

The summary of the data from the study of various physical properties of  $Li_2O$ -CaF<sub>2</sub>-P<sub>2</sub>O<sub>5</sub>: Cr<sub>2</sub>O<sub>3</sub> glass cera-

mics is as follows: The optical absorption and ESR spectral studies indicate that there is a gradual conversion of chromium ions from Cr<sup>3+</sup> state to Cr<sup>6+</sup> state as the concentration of the nucleating agent is increased from 0.4 to 0.8 mol%. The presence of chromium ions in  $Cr^{4+}$  and Cr<sup>5+</sup> states could also be felt from these studies. The glassceramic samples crystallized with 0.4 mol% Cr<sub>2</sub>O<sub>3</sub> (in which chromium ions exists predominantly in  $Cr^{3+}$  state) exhibited high luminescence emission and hence these samples may be considered as more efficient luminescence materials. Though a part of the chromium ions seems to exist in  $Cr^{4+}$  state in the sample  $C_8$ , that give laser emission in the NIR range, but their concentration is very low and further there is a possibility of high non-radiating or phonon losses in this sample. The dielectric studies indicate the highest insulating strength for the sample C<sub>8</sub> and the a.c. conduction in the samples  $C_2$  and  $C_4$  is primarily ionic in nature.

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